INFLUENCE OF MOSFET MODEL FORM ON CHARACTERISTICS OF THE BOOST CONVERTER

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Abstract: In the paper boost converter characteristics at the steady state obtained from SPICE analysis with the use of selected kinds of MOSFET models of various complexity and accuracy are compared. The dependencies of the converter output voltage, the watt-hour efficiency and the MOSFET inner temperature on the frequency and the duty cycle of the MOSFET control signal as well as the converter load resistance are considered. The correctness of the calculation results was verified experimentally. The duration time of the analyses corresponding to all the considered models of the MOS transistor are compared, too.

1. Introduction

Dc-dc converters are commonly used in power supply systems /1/. The boost converter is the most popular in the class of step-up converters of the output power up to 1 kW. The network representation of the boost converter with the MOS power transistor operating as the switch is shown in Fig.1.

![Fig. 1. The diagram of a boost converter](image)

The analysis and design of electronic circuits e.g. dc-dc converters requires the use a proper computer tool (algorithms). To this end SPICE is the appropriate tool /2, 3/. The accuracy and duration time of calculations depend among others on the form of models of semiconductor devices and elements existing in the considered circuit.

The characteristics describing dc-dc converters at the steady state have a fundamental significance for the engineer-designer of such a class of circuits. Two groups of methods of the analysis of dc-dc converters at the steady state can be distinguished. The first method is based on the dc analysis with average models of the analysed circuit taken into account /4-8/, whereas in the other method based on the transient analysis, the large-signal dynamic models of devices operating in the circuit are used /2, 4, 7, 9/. As it was shown in /10/, the second method allows obtaining much better consistency between the calculation and measuring results, but the analysis duration time can be much longer than in the first method.

There are models of different accuracy, among of both kinds of models mentioned before. For example, in the paper /11/ the results of the analysis of the isolated dc-dc converter obtained by nonlinear inertial models of the Schottky diode and the MOS transistor are presented. In turn, the paper /12/ presents the results of a small-signal analysis of the buck-boost converter obtained with the use of devices models of the form of ideal switches. In the paper /13/ the results of the analysis of the dc-dc converter obtained by the SPICE built-in models of the diode and the MOS transistor were used as the reference results to verify the correctness of the new method of calculations of converter characteristics. The description of the behavioral dc-dc converter models of different accuracy dedicated to the system level analysis can be found in /14/. The similar meaning is to be found in the models presented in the paper /15/, whose parameters values can be estimated with the use of the catalogue data of converter devices. The paper /16/ describes the method of estimation of the electrothermal characteristics of dc-dc converters with the...
use of the method of the separated iteration with the use of nonlinear semiconductor devices models. The nonlinear models of semiconductor devices were also used in the analysis of a dc-dc converter in the small-signal /17/ and large-signal /18/ case, respectively. The average models of dc-dc converters with nonlinearities of semiconductor devices taken into account are described in /19, 20/.

The aim of this paper, being of the extended version of the paper /21/, is to estimate the influence of the form of the MOS transistor model on the boost converter characteristics at the steady state obtained by the transient analysis. The analyses were performed by SPICE with the use of SPICE built-in linear models of: the inductor \( L \), the capacitor \( C \), the resistors \( R_p \), \( R_s \), the voltage sources \( V_{in}, V_{on} \) and the model of the diode D1 described in /22/. Five various models of MOS transistor were tested. Namely: the model of the ideal switch, the Dang’s model built-in in SPICE, the two-value resistor model, the electrothermal model of the two-value resistor /23/ and the electrothermal hybrid model of the considered device /24/. The results of the analysis of the form of the proper characteristics of the boost converter and the duration time of the analyses performed with the use of the above mentioned MOS transistor models are presented and compared. The calculations were performed in the wide range of variations of the duty cycle \( D \) and the frequency \( f \) of the control signal as well as the load resistance \( R_0 \). Some results of the analyses were compared with the results of measurements.

2. MOSFET models used in analyses

The simplest model of the MOS transistor, among the considered models, is the ideal switch model, whose switch-on and switch-off resistances are equal to zero and infinity, respectively. The main drawback of this model is discontinuity of their characteristics, which can result in the problem of the lack of calculations convergence. Such a model cannot be directly implemented in SPICE. On the other hand, the SPICE built-in model of the voltage controlled switch (VSWITCH) with switch-on and switch-off resistances of the values, which tend to be zero and infinity, respectively, can be used.

The second in turn considered model is the two-value resistor model, which possesses non-zero value resistance in the on-state \( R_{ON} \) and the finite value of the resistance in the off-state \( R_{OFF} \). In this model the values of the resistances \( R_{ON} \) and \( R_{OFF} \) are independent of temperature.

These models are formulated in SPICE with the use of the model of the voltage controlled switch, the characteristics of which are described by the four parameters: the resistances \( R_{ON}, R_{OFF} \) and the voltages \( V_{ON}, V_{OFF} \) — representing the device gate-source voltage at the device on-state and off-state, respectively.

The third model of the MOS transistor is the electrothermal model of the switch /24/. This model is an improved version of the two-value resistor model, in which the influence of the ambient temperature and the selfheating phenomenon on the resistance \( R_{ON} \) are included. This model, the network representation of which is shown in Fig.2, is composed of two elements connected in series: the SPICE built-in model of the voltage controlled switch \( S1 \) (the two-values resistor) and the voltage controlled source \( E_{RON} \) described by the formula

\[
E_{RON} = V_S \cdot \alpha_{RON} \cdot (R_{ON} \cdot I - T_a + T_h)
\]

where \( V_S \) denotes the voltage on the two-values resistor, \( V_{S1} \) — the voltage on the switch \( S1 \), \( T_a \) — ambient temperature, \( R_{ON} \) — the thermal resistance of the transistor, \( I \) — the current of the two-value resistor, \( \alpha_{RON} \) — the temperature coefficient of variations of the on resistance of the two-values resistor. The resistance of the switch-on switch \( S1 \) is equal to the resistance \( R_{OM} \), corresponding to the on-resistance of the two-values resistor at the reference temperature \( T_o \).

![Fig.2. The network representation of the two-values resistor model](image)

Both the electrical inertia and nonlinearity of the device current-voltage characteristics are not included in the presented models.

The next is the Dang’s isothermal model of the MOS transistor built-in in SPICE, described e.g. in /22/. This model takes into account the nonlinear d.c. characteristics and the inertia of the considered device, whereas the selfheating phenomenon is not taken into account in this model. There are 28 parameters describing the Dang’s model /22/. These parameters are: model index (LEVEL), default channel length (L), default channel width (W), drain ohmic resistance (RD), source ohmic resistance (RS), gate ohmic resistance (RG), bulk/substrate ohmic resistance (RB), zero-bias bulk-drain junction capacitance (CBD), zero-bias bulk-source junction capacitance (CBS), bulk junction saturation current (IS), Bulk junction saturation current per sq-meter of junction area (JS), Bulk junction saturation current per length of sidewall area (JSSW), bulk junction emission coefficient (N), bulk junction potential (PB), bulk junction sidewall potential (PBJSW), gate-source overlap capacitance per meter channel width (CGSO), gate-drain overlap capacitance per meter channel width (CGDO), gate-bulk overlap capacitance per meter channel length (CGBO), drain and source diffusion sheet resistance (RSH), Zero-bias bulk junction bottom capacitance per square meter of junction area (CJ), zero-bias bulk junction sidewall capacitance per length of sidewall (CJSW),
bulk junction bottom grading coefficient (MJ), zero-bias bulk junction sidewall capacitance per meter of junction perimeter (CJSW), bulk junction sidewall grading coefficient (MJSW), bulk junction transit time (TT), flicker noise coefficient (KF), flicker noise exponent (AF), coefficient for forward-bias depletion capacitance formula (FC), zero-bias threshold voltage (VTO), transconductance parameter (KP), bulk threshold parameter (GAMMA), surface potential (PHI), oxide thickness (TOX), substrate doping (NSUB), surface state density (NSS), fast surface state density (NFSS), type of gate material (TPG), metallurgical junction depth (XJ), lateral diffusion (LD), lateral diffusion width (WD), surface mobility (UM), critical field for mobility degradation (UCRIT), critical field exponent in mobility degradation (UEXP), transverse field coefficient (UTRA), maximum drift velocity of carriers (VMAX), total channel charge coefficient (NEFF), thin-oxide capacitance model flag and a fraction of channel charge attributed to drain (XQC), width effect on threshold voltage (DELTA). Table 1. The values of parameters of the considered MOS transistor IRF840 models

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>ToX</td>
<td>500</td>
</tr>
<tr>
<td>PHI</td>
<td>0.6 V</td>
</tr>
<tr>
<td>RS</td>
<td>6.382 mΩ</td>
</tr>
<tr>
<td>KP</td>
<td>20.85 μA/V²</td>
</tr>
</tbody>
</table>

In the considered MOS transistors models the values of the parameters collected in Table 1 were used.

The boost converter (Fig.1) with transistor IRF840, the diode BY229, the inductor of inductance 650 μH, and the capacitor of capacitance 47 μF was investigated.

In the considered MOS transistor IRF840 models, the values of the parameters collected in Table 1 were used.

In Fig.4 the calculated and measured output characteristics $i_D(v_{DS})$ of the transistor IRF840 at $v_{GS} = 15$ V are presented. This figure (and in the further ones) the points denote the measuring results, whereas the lines – the results of the analysis. In Fig.4 the following notations are used: a – the electrothermal hybrid model of the considered transistor, b – the isothermal built-in in SPICE Dang’s model, c – the ideal switch model, d – the isothermal model of the two-
value resistor, e - electrothermal model of the two-value resistor.

As seen from Fig.4, the characteristic corresponding to the ideal switch (the characteristic c covers the vertical axis of ordinates) differ essentially from the remaining characteristics (curves a, b, d, e). In turn, the characteristics calculated with the device isothermal model (curve b) and with the model of two-value resistor (curve d) are practically identical and linear in the considered range of variations of the drain current. The characteristics corresponding to the models including selfheating (the curves a and e) are nonlinear and practically overlap. The characteristics a and e show that selfheating evidently results in an increase of the device resistance $R_{ON}$.

3. Results

Using the considered models of the MOS transistor (Section II) the transient analysis of the boost converter (Fig.1) up to the steady state for various values of the load resistance $R_0$, the duty cycle $D$ and the frequency $f$ of the device control signal, was performed. The influence of these parameters ($R_0$, $D$, $f$) on the output voltage and the watt-hour efficiency of the converter as well as the MOS transistor case temperature was investigated. During the measurements the MOS transistor and the diode were situated on the heat-sinks. The value of the thermal resistance of the MOS transistor measured with the use of the measuring method from /25/ and the measuring set described in /26/ is equal to 5.5 K/W. The measurements of characteristics were carried out by typical multimeters at the thermal steady-state, whereas the device case temperature was measured by the pyrometer ST-3. In the analysis the SPICE built-in isothermal model of the p-n diode with the following parameter values (corresponding to the diode BY229): $I_s = 53.4 \, \mu A$, $N = 1.185$, $R_S = 0.12 \, \Omega$, $\alpha_{s1} = 3 \cdot 10^{-3}$, $I_{k1} = 3.5 \, \mu A$, $C_{j0} = 325 \, \mu F$, $M = 0.3333$, $V_J = 0.75 \, V$, $F_c = 0.5$, $I_{sr} = 100 \, \mu A$, $N_m = 2$, $T_T = 145 \, ns$ was used. In the analysis the inductor series resistance of the value equal to 0.1 $\Omega$ was taken into account.

The transient analyses of the considered circuit until the steady-state were performed with the use of all the models described in Chapter III. The calculated values of the converter output voltage $V_{out}$, the watt-hour efficiency $\eta$, and the case temperature $T_c$ are shown in Figs. 5 -7.

In Fig.5 the results of the calculated and measured dependences of the output voltage and the watt-hour efficiency of the converter and the transistor case temperature (c) on the duty-factor of the control signal $K$. Górecki, J. Zarebski: Influence of Mosfet Model Form on Characteristics of the Boost Converter Informacije MIDEM 41(2011)1, str. 1-7

As seen from Fig.5, the results of analysis with the use of the electrothermal hybrid model of the MOS transistor (curve a) and the electrothermal model of the two-values resistor (curve e) fit well to the measuring results. Neglecting the selfheating phenomenon in the MOS transistor (curves b and d) results in too high values of the converter output voltage and shifts of the maximum on the characteristic $V_{out}(D)$ towards the higher values of the coefficient $D$. In turn, neglecting conducting losses in the transistor (curve c) results in a considerable increase of the converter output voltage. It is worth mentioning that the differences between the values of the voltage $V_{out}$ obtained with the use of all the considered models are hardly visible at small values of the coefficient $D$ ($D < 0.4$). Moreover, these differences increase with an increase of $D$.

As seen from Fig.5b the dependence $\eta(D)$ is a decreasing function. The best agreement between the analysis and measuring results is assured by the MOS transistor models with a electrical inertia and selfheating taken into account.
(curves a, b, d, e). Disregarding conducting losses in the MOS transistor results in a considerable increase of the watt-hour efficiency of the converter.

It results from Fig. 5c that the case temperature $T_{CT}$ of the MOS transistor is an increasing function of the coefficient $D$ and the values of $T_{CT}$ obtained with the use of the both electrothermal models (curves a and e) fit well to the measurements.

In Fig. 6 the calculated and measured values of the converter output voltage (Fig. 4a) and the watt-hour efficiency (Fig. 4b) as well as the MOS transistor case temperature (Fig. 4c) on the converter load resistance at $D = 0.5$ and $f = 100 \text{ kHz}$ are presented.

![Image of Fig. 6](image-url)

**Fig. 6.** The calculated and measured dependences of the converter output voltage (a) and the watt-hour efficiency (b), as well as the transistor case temperature (c) on the load resistance.

Fig. 6a shows that the converter output voltage is an increasing function of the resistance $R_0$. In the range of small values of the load resistance ($R_0 < 2 \Omega$) the considered converter operates incorrectly, that means that $V_{\text{out}} < V_{\text{in}}$.

It results from Fig. 6b that a decrease of the resistance $R_0$ leads to a decrease of the converter watt-hour efficiency. It is worth mentioning that the dependences $\eta (R_0)$ obtained with the use of the models taking into account the MOS transistor conducting losses (curves a, b, d, e) have local minimums and local maximums (peaks) at the load resistance values in the range from 0.5 $\Omega$ to 2 $\Omega$. Neglecting the conducting losses in the MOS transistor results in an increase of both the output voltage and the watt-hour efficiency of the converter even more than 50%.

Fig. 6c shows that the measured values of the case temperatures of the MOS transistor fit well to the calculated values at $R_0 < 1.5 \Omega$ only. The measured characteristic $T_{CT}(R_0)$ is a monotonically decreasing function, whereas the same characteristic obtained from the calculations has the peak at $R_0 = 1.5 \Omega$.

In Fig. 7 the influence of the frequency $f$ of the signal controlling the MOS transistor on the converter output voltage (Fig. 7a) and the watt-hour efficiency (Fig. 7b) as well as the case temperature of the MOS transistor (Fig. 5c) is presented. The calculations and measurements were performed at $D = 0.75$ and $R_0 = 20 \Omega$.

It results from Fig. 7a that the voltage $V_{\text{out}}$ is a decreasing function of the frequency $f$. This dependence is described correctly by the electrothermal hybrid model of the MOS transistor (curve a) only. The values of the voltage $V_{\text{out}}$ obtained from the remaining models are inflated. For the signal frequency $f > 1 \text{ MHz}$ the investigated converter does not operate correctly due to too high values of the MOS transistor inner capacitances, which make the proper switching of the MOS transistor impossible. The values of the voltage $V_{\text{out}}$ corresponding to this range of the signal frequency are equal to the difference of the converter input voltage and the voltage drop on the forward biased diode D. As seen, the model of the two-value resistor ensures the correct values of the voltage $V_{\text{out}}$ if the signal frequency is less than 150 kHz only.

It results from Fig. 7b that increasing of the signal frequency $f$ causes increasing of the converter watt-hour efficiency up to a few percentage only in the range of the frequency $f > 1 \text{ MHz}$. This phenomenon is observed from the calculation results obtained with the use of all the considered models, because in all the analyses the diode inertia is taken into account.

Fig. 7c shows that the electrical power dissipated while switching the MOS transistor influences substantially the device case temperature $T_{CT}$ in the range of higher values of the frequency of the MOS transistor controlling signal. The values of the temperature $T_{CT}$ obtained with the use of both the considered electrothermal models differ from each other even more than 30%. The temperature $T_{CT}$ doubles when the signal frequency $f$ increases from 100 kHz to 5 MHz.
Apart from the model accuracy, the time of the converter analysis with the use of these models gives also very important information about the usefulness of the models. Table 2 compares the times (in seconds) of the analysis of the boost converter with the use of the considered MOS transistor models.

As seen from Table 2, in the range of small values of the frequency of the control signal, the isothermal model of the two-value resistor ensures the shortest time of the analysis – more than twice shorter than the analysis time with the use of the hybrid electrothermal model. In turn, in all the considered range of variations of the frequency f, the isothermal built-in model of the MOS transistor is the best from the point of view of the analysis rate. In this case the time indispensable for the analysis is twice lower than in the case, when the models of the ideal switch or two-values resistance are used. It is worth mentioning that the model of the worst accuracy (the model of the ideal switch) does not ensure the shortest time of the analysis. This results from the fact, that during switching of the non-inertia switch, very fast changing of the currents and voltages are observed. In a consequence, the time derivatives of currents and voltages of the high values appear, what results in shortening of the calculating step. Finally, the time of analysis have to be increased.

4. Conclusions

In the paper the influence of the model form of the MOS transistor on the characteristics of the boost converter is investigated. As results from the investigations performed by the authors, using the device electrothermal hybrid model ensures a good agreement between the calculated and measured characteristics of the considered dc-dc converter in the wide range of variations of the load resistance, the duty-factor and the frequency of the control signal of the MOS transistor.

If the control signal frequency is less than 150 kHz, then the electrothermal model of the two-value resistor ensures a good agreement between the calculation and measurement results and moreover the analysis time is twice shorter than in the case of the use of the electrothermal hybrid model of the MOS transistor.

For the low values of the MOS transistor control signal frequency and small values of the converter load resistance, selfheating has to be included in the model, whereas it is indispensable for the high values of the control signal frequency to take to account the MOS transistor electrical inertia.

The presented results of the boost converter investigations show that for the control signal frequency less than 150 kHz the inertia can be omitted in the devices models, whereas the static losses in these devices at the on-state

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Hybrid electrothermal model</th>
<th>Isothermal built-in model</th>
<th>Ideal switch</th>
<th>Two-value resistor</th>
<th>Electrothermal two-value resistor</th>
</tr>
</thead>
<tbody>
<tr>
<td>$V_{out}(D)$</td>
<td>161.77 s</td>
<td>125.83 s</td>
<td>70.28 s</td>
<td>67.11 s</td>
<td>87.17 s</td>
</tr>
<tr>
<td>$V_{out}(R_o)$</td>
<td>366.05 s</td>
<td>289.55 s</td>
<td>148.10 s</td>
<td>126.06 s</td>
<td>165.24 s</td>
</tr>
<tr>
<td>$V_{out}(f)$</td>
<td>281.08 s</td>
<td>232.69 s</td>
<td>513.84 s</td>
<td>418.22 s</td>
<td>504.78 s</td>
</tr>
</tbody>
</table>
play the essential role. Therefore a very important challenge would be working out an electrothermal large-signal model of the transistor switch with the inertia phenomena taken into account.

References


K. Górecki, J. Zarębski: Influence of Mosfet Model Form on Characteristics of the Boost Converter
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